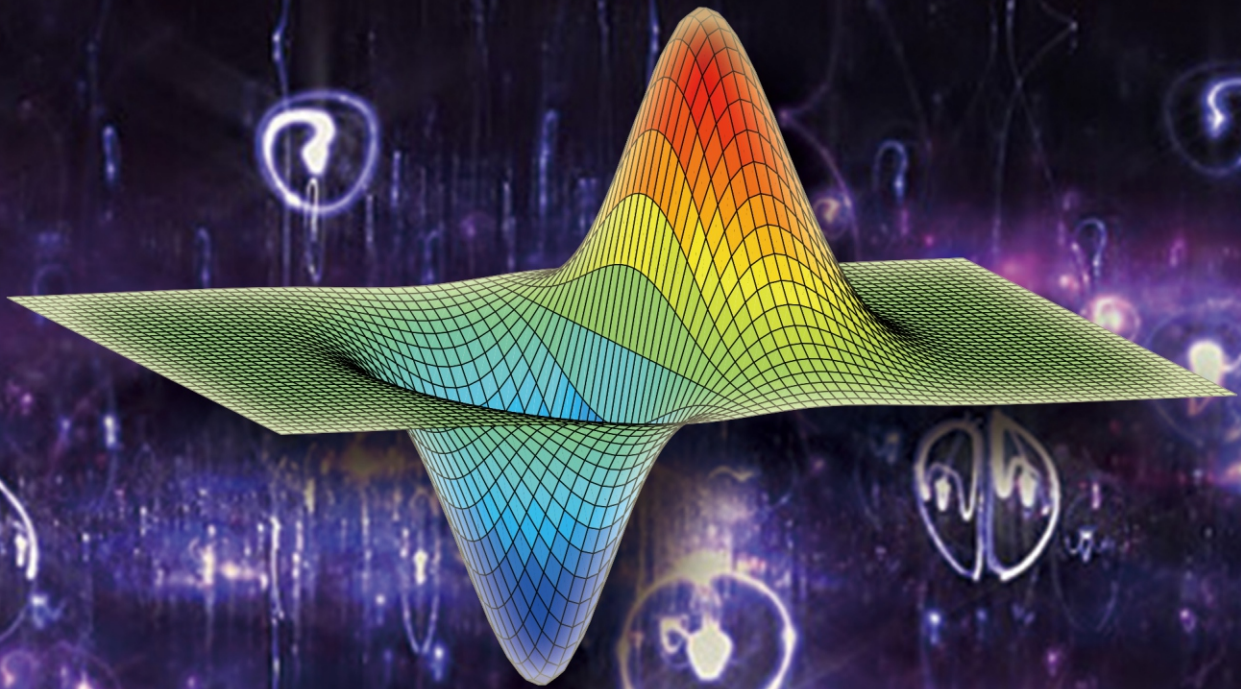


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Table of Contents

Volume 15 Number 11

November 2025

Bifurcations and Traveling Wave Solutions of a Generalized b-Family of Novikov Equation

C. Wei, H. Su, X. J. Zhao 711

An Infinite Series Expression for the Joint Probability Density Function of Occupation Times in a Three-State Markov Chain

J. Evans, A. Korzeniowski 718

Comprehensive Analysis of Complex Products in Groups: From Elementary Combinatorics to Advanced Structural Theory

A. Gonchar 726

Vector-Valued Convex Functions

M. Laayouni 743

On Matrix Strong Diophantine 540-Tuples, Matrix Elliptic Curves and Matrix Hyperelliptic Curves

D. Dehainsala, J. M. Mouanda 751

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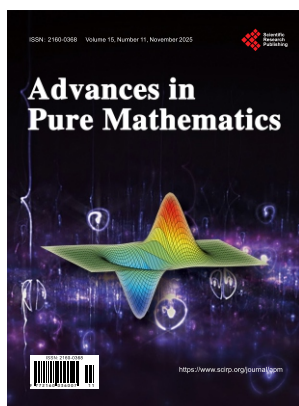
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