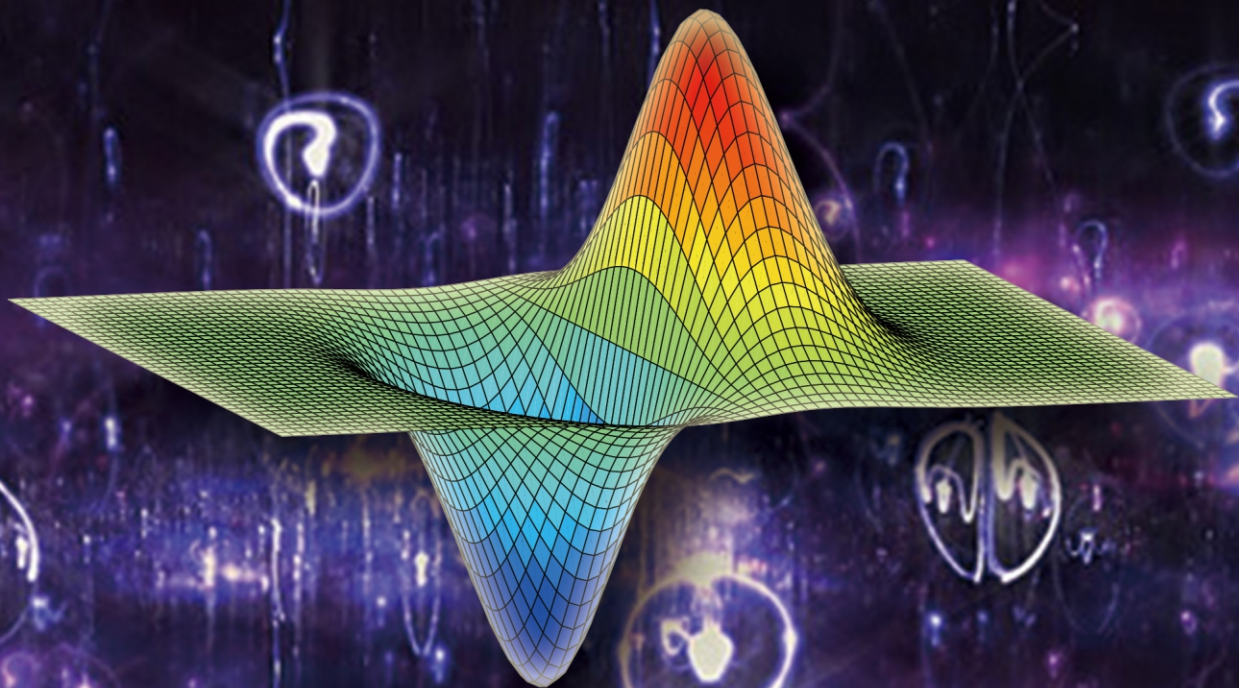


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# Table of Contents

**Volume 10    Number 9**

**September 2020**

**Monte Carlo Simulations of Topological Properties in Two-Phase Polycrystalline Materials  
for Several Diffusion Mechanisms**

R. J. El-Khozondar.....471

**A Growth Behavior of Szegő Type Operators**

J. Yang.....492

**Some Theorems for Real Increasing Functions in Elementary Fixed Point Theory**

M. L. Diviccaro, S. Sessa.....501

**A New Understanding on the Problem That the Quintic Equation Has No Radical Solutions**

X. C. Mei.....508

**Solutions of Indefinite Equations**

Z. Y. Liang.....540

**Erratum to “Valid Geometric Solutions for Indentations with Algebraic Calculations”,  
[Advances in Pure Mathematics, Vol. 10 (2020) 322-336]**

G. Kaupp.....545

**Clarifications for the Published Article: “A Solution to the Famous Twin’s Problem”  
in the APM of SCIRP at 24 September of 2019**

P. C. Papadopoulos.....547

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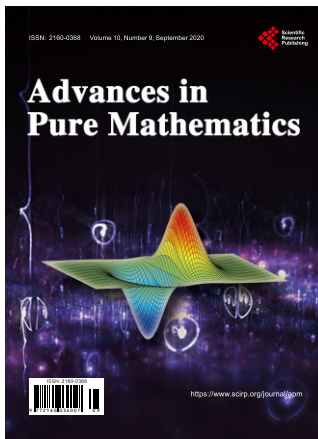
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